

Chapter 7:
Techniques of Integration

Section 7.1:
Integration By Parts

Sec. 7.1: Integration by Parts

The Integration by Parts Formula...

$$\int u dv = uv - \int v du$$

Notes:

- You must be integrating a product to use integration by parts
- You want the new integral to be easier to do than your original integral

Sec. 7.1: Integration by Parts

Ex 1: Find $\int x e^x dx$

Sec. 7.1: Integration by Parts

Ex 2: Find $\int t^3 \sin(t) \, dt$

Sec. 7.1: Integration by Parts

Ex 3: Find $\int e^x \cos(x) dx$

Sec. 7.1: Integration by Parts

Ex 4: Find $\int \ln(x) \, dx$

Sec. 7.1: Integration by Parts

Ex 5: Find $\int_0^1 \sin^{-1} x \, dx$

Sec. 7.1: Integration by Parts

Ex 6: Find $\int e^{\sqrt{x}} dx$

Sec. 7.1: Integration by Parts

Ex 7: Prove the reduction formula

$$\begin{aligned} \int \sin^n(x) \, dx &= \\ &= -\frac{1}{n} \cos(x) \sin^{n-1}(x) + \frac{n-1}{n} \int \sin^{n-2}(x) \, dx \end{aligned}$$

where n is an integer and $n \geq 2$.